

数学与系统科学研究院

计算数学所学术报告

报告人: 赵璇 博士

( 东南大学数学系 )

报告题目:

**Second-order approximations for  
variable order fractional derivatives:  
Algorithms and applications**

邀请人: 唐贻发 研究员

报告时间: 2014 年 10 月 30 日 (周四)

下午 16:00-17:00

报告地点: 数学院南楼七层 702  
会议室

## **Abstract:**

**Fractional calculus allows variable-order of fractional operators, which can be exploited in diverse physical and biological applications where rates of change of the quantity of interest may depend on space and/or time. We derive two second-order approximation formulas for the variable-order fractional time derivatives involved in anomalous diffusion and wave propagation. We then present numerical tests that verify the theoretical estimates of convergence rate and also simulations of anomalous sub-diffusion and super-diffusion that demonstrate new localized diffusion rates that depend on the curvature of the variable-order function. Finally, we perform simulations of wave propagation in a truncated domain to demonstrate how erroneous wave reflections at the boundaries can be eliminated by super-diffusion, and also simulations of the Burgers equation that serve as a testbed for studying the loss and recovery of monotonicity using again variable rate diffusion as a function of space and/or time. Taken together, our results demonstrate that variable-order fractional derivatives can be used to model the physics of anomalous transport with spatiotemporal variability but also as new effective numerical tools that can deal with the long-standing issues of outflow boundary conditions and monotonicity of integer-order PDEs.**

**欢迎大家参加!**