

数学与系统科学研究院

计算数学所学术报告

报告人: **Prof. Arieh Iserles**

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报告题目:

**Skew-symmetric differentiation  
matrices and spectral methods on the  
real line**

邀请人: 洪佳林 研究员

报告时间: **2018 年 10 月 10 日 (周三)**

**下午 16:00-17:00**

报告地点: 数学院南楼二层

**222 教室**

## **Abstract:**

A most welcome feature of orthogonal bases employed in spectral methods is that their differentiation matrix is skew symmetric, since this makes energy conservation automatic in conservative time-evolving problems. A familiar example is given by Hermite functions, which are dense in  $L^2(-\infty, \infty)$  and give rise to a skew-symmetric, tridiagonal differentiation matrix.

In this talk, describing joint work with Marcus Webb (KU Leuven), we present full characterisation of all orthogonal systems acting on  $L^2(-\infty, \infty)$ , dense either there or in a Paley—Wiener space, and that have a differentiation matrix which is skew-symmetric, tridiagonal and irreducible. We also present a constructive algorithm for their generation — essentially, given any symmetric Borel measure on  $(-\infty, \infty)$  or on  $(-a, a)$  for some  $a > 0$ , there exists a unique (up to rescaling) basis of this kind and it can be generated constructively. We conclude with a number of examples, related to Konoplev, Carlitz and Freud measures.

Finally, we address the more general question of skew-Hermitian differentiation matrices. This brings us to very recent work on a variant of Malmquist—Takenaka basis, which appears to tick every desirable box: an orthonormal system dense in  $L^2(-\infty, \infty)$ , with tridiagonal skew-Hermitian differentiation matrix and whose generalised Fourier coefficients can be computed with a single FFT.

**欢迎大家参加！**