

数学与系统科学研究院  
计算数学所定期学术报告

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报告题目:

**C0 elements for computational  
electromagnetism**

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**计算数学所报告厅**

## **Abstract:**

I will talk about the application of  $C_0$  elements for computational magnetism. As is well-known, electromagnetism is governed by curl and div operators. A natural finite element method for this type of curl-div equations should be  $C_0$  element method, since both curl and div conforming piecewise polynomial approximations are necessarily  $H_1$  conforming and are thus  $C_0$  elements. However, it is by no means seemingly correct for  $C_0$  elements in solving curl-div equations. In fact, it had been for more than half a century no advances were known about whether  $C_0$  elements could be employed for the curl-div equations or not. A well-known fact had been that  $C_0$  elements failed whenever the domain is nonsmooth with reentrant corners and edges or whenever the solution is nonsmooth and does not belong to  $H_1$  space. Until 2002, a breakthrough was made by Costabel and Dauge, with a weighted-regularization method for Maxwell's equations. Since then, several new variants and new  $C_0$  element methods have been developed. The new variants of the weighted regularization  $C_0$  element methods are two. Jr. Ciarlet and his research group study a weighted regularization mixed  $C_0$  element method. T. Manteuffel and his research group study a weighted least-squares  $C_0$  finite element method for first-order system. Beside the weighted regularization  $C_0$  element method, the new  $C_0$  element methods are also two. J. Bramble and his research group propose a minus one norm based least-squares  $C_0$  finite element method for first-order system. H. Duan and his research group propose and develop a  $L_2$  projected  $C_0$  element method for any curl and div equations including second-order and first-order systems. J.-L. Guermond and his research group study a variant of the minus one norm based  $C_0$  element method for curl-div equation by applying the minus one norm to measure the first-order div equation like in the first-order system.  $C_0$  element methods are very attractive, especially when applied to magnetohydrodynamic where Navier-Stokes equations are coupled with Maxwell's equations, since all the unknowns can be approximated using the same type of  $C_0$  elements. In the form of first-order system,  $C_0$  elements are particularly useful, one mesh, one element, one code and one algorithm for all matters in computer realization. In this talk, several numerical examples will be given to illustrate our  $L_2$  projected  $C_0$  element methods for curl and div equations related to Maxwell's equations. In conclusion, so far, there are three  $C_0$  element methods, 1) weighted  $C_0$  element method; 2)  $H^{-1}$   $C_0$  element method; 3)  $L_2$  projected  $C_0$  element method.

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