

数学与系统科学研究院

计算数学所学术报告

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报告题目:

**Regularized weighted least squares
approximation by orthogonal
polynomials**

邀请人: 许志强 研究员

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报告地点: 数学院南楼二层

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Abstract:

We consider polynomial approximation over the interval $[-1,1]$ by a class of regularized weighted discrete least squares methods with ℓ_2 -regularization and ℓ_1 -regularization terms, respectively. It is merited to choose classical orthogonal polynomials as basis sets of polynomial space with degree at most L . As node sets we use zeros of orthogonal polynomials such as Chebyshev points of the first kind, Legendre points. The number of nodes, say $N+1$, is chosen to ensure $L \leq 2N+1$. With the aid of Gauss quadrature, we obtain approximation polynomials of degree L in closed form without solving linear algebra or optimization problem. As a matter of fact, these approximation polynomials can be expressed in the form of barycentric interpolation formula when the interpolation condition is satisfied. We then study the approximation quality of ℓ_2 -regularization approximation polynomial, especially on the Lebesgue constant. Moreover, the sparsity of ℓ_1 -regularization approximation polynomial, respectively. Finally, we give numerical examples to illustrate these theoretical results and show that well-chosen regularization parameter can provide good performance approximation, with or without contaminated data.

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